



# Performance Evaluation of Fixed Bed Column Packed with Ionic Liquid Impregnated Silica for Separation of Gadolinium and Neodymium from Aqueous Solutions

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## Abstract

Application of fixed bed column for separation of gadolinium and neodymium ions from their aqueous solutions using cyphos IL-104 impregnated silica was investigated. The performance of separation of the two lanthanide elements was evaluated by determining the column capacity, the total quantity sorbed of metal ions, and the removal percentage. These indicative column performance parameters were evaluated in altered conditions including fixed bed height of 2.0 and 3.0 cm, flow rate of 1.0 and 2.0 mL/min, and solution feed concentration of 50 and 100 ppm. Breakthrough modeling of the sorption process across the column was performed by employing Thomas and Adams–Bohart models. It was found that it took less time to reach the breakthrough when the flow rate and initial concentration increased, while the height of the bed decreased. Also, the column capacity increased by increasing the bed depth, decreasing the flow rate, and increasing the initial metal ion concentrations. 0.1 M nitric acid was found to be the best media for the separation of Nd<sup>3+</sup> and Gd<sup>3+</sup> ions.

**Keywords** Separation · Impregnation · Nd<sup>3+</sup> and Gd<sup>3+</sup> · Fixed bed column · Modeling

## Introduction

The batch technique is important in providing information about the efficiency of metal-sorbent system, but the obtained data are not sufficient for applying this technique to a large scale in the most treatment processes, specially, in continuous-flow mode. Therefore, this study is interested in using the column technique for separation of gadolinium and neodymium ions from their aqueous solutions.

Lanthanide elements enter the environment via various pathways due to the rapid increase of the use of their resources and applications in several fields of modern industry and daily life. Toxicological research has shown

that lanthanides can have serious harmful effects on living organisms [1]. In environmental studies, Lanthanides' deposition in water, food chain, and soil must be regarded [2]. Radioisotope of neodymium (light lanthanide element) is used to monitor nuclear fuel utilization [3], as well as its applications in coloring glass, doping glass, lasers, and many electronic devices [4]. Gadolinium (heavy lanthanide element) is used in the nuclear power plant as shielding device to minimize the interaction of thermal neutrons with materials. Gadolinium has application in radiochemical analysis in the determination of the extent of burn-up of nuclear fuels (as <sup>154</sup>Gd-<sup>157</sup>Gd) [5]. Also enters in various applications like lamp phosphors, optical glass, and permanent magnets [6, 7]. Separating and recycling lanthanide components from nuclear and industrial waste are critical for both environment and economy [8–11]. There are different technologies or processes used for radioactive waste treatment based on achieving these goals such as adsorption, chemical precipitation, solvent extraction, membrane process, and ion exchange [12–21]. Sometimes, a combination of several processes can be used to provide effective treatment of a liquid waste stream. Immobilizing an extractant in a resin support allows maintaining their high recovery efficiency

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and preventing their dispersion in the aqueous solution (expensive and hazardous compounds) [22]. Additionally, the presence of the resin may enhance the removal efficiency of the extractant [23].

Recovery of solvent extractant immobilized sorption in a fixed bed is an unsteady-state process, involving the accumulation of solute molecules onto a sorbent from a solvent crossing the column.

Sorption using a fixed bed is broadly used in practical industrial applications for purification and separation purposes. The performance of fixed bed column is evaluated by testing the breakthrough curve of the sorption. To explain and forecast the breakthrough curves, a number of mathematical models have been established [24].

This work focused on evaluation of performance of fixed bed column for removal and separation of neodymium and gadolinium ions from aqueous solution. The studied fixed bed column is packed with Cyphos IL-104 impregnated on silica. Thomas and Adams–Bohart models were used to accomplish this evaluation.

## Experimental

### Materials and Methods

Ionic liquid, namely trihexyl (tetradecyl) phosphonium bis-2, 4,4-(trimethylpentyl) phosphinate, Cyphos IL-104, was purchased from Fluka. Grade 62 Silica gel, 150 Å was obtained from Sigma-Aldrich.  $\text{NH}_4\text{OH}$ ,  $\text{HNO}_3$ , and  $\text{HCl}$  from Winlab. Neodymium and Gadolinium nitrates from Merck. Chemicals and reagents are of analytical grade.

### Column System

The dimensions of the glass column used in this study were 15 cm length and 1 cm inner diameter. A 2.0 mm-thick disc of glass wool is incorporated in the bottom and the top of the column to prevent leakage. For the accuracy of the results, this glass wool verified not to adsorb any weighty amounts of the metal ions from the solution. Impregnated silica, cyphos@silica, was used as a sorbent material. The material was prepared as the same description illustrated in our previous work [2]; where silica was impregnated by an ionic liquid, Cyphos IL-104, as follows: 50% loading percent was achieved by adding 2.0 mL of Cyphos IL-104 to 4 g of silica followed by stirring overnight in the presence of ethanol (few drops). The resulting homogenous mixture was filtered followed by washing with distilled water to eliminate excess solvent. The product (cyphos@silica) was subjected to overnight drying in an air oven at temperature of  $333 \pm 1$  K. The resin (cyphos@silica) was packed through the column. The column was routinely preconditioned with

water at a definite flow rate [25]. The metal ion solutions, at optimum pH equals 3.5, were fed into the column. The feeding flow rate was adjusted by a pump connected to the column. The effluent volumes passed throughout the column were collected in known fraction volumes for spectrophotometric measurements. The separation experiment of the two metal ions from their binary solutions was carried out at defined flow rate and bed size. Different concentrations of nitric acid were tested for the elution to find out the optimum concentration for the separation of the two studied  $\text{Nd}^{3+}$  and  $\text{Gd}^{3+}$  ions.

## Results and Discussion

From the previous work, batch equilibrium results [2], it is clear that both neodymium and gadolinium ions can be effectively removed from aqueous solution by Cyphos@silica material. The sorption using column technique was investigated to evaluate the practical usefulness of Cyphos@silica material for sorption of neodymium and gadolinium from their solutions. The fixed bed column performance presented using breakthrough curves. The breakthrough curve display concentration ratios  $C_t/C_0$  as a function of effluent volumes ( $C_v$ ), mg/L where  $C_t$  is the effluent concentration of neodymium and gadolinium and  $C_0$ , mg/L is the initial concentration. When the concentration of effluent,  $C_t$ , is equal to that of feed concentration,  $C_0$  (i.e.,  $C_t/C_0 = 1$ ) that is an indication of reaching saturation of the column [26]. The column beads were pre-conditioning by washing them with 100 mL distilled water to remove all air bubbles from the column bed. After that, the neodymium and gadolinium solutions passing through the column at optimum pH = 3.5 deduced from batch results [2]. The column performance can be investigated by studying some factors, such as height of the fixed bed, flow rate, and the initial concentration of metal ion solution [27, 28].

### Effect of Bed Depth

Different bed depths of 2 and 3 cm were used to investigate the effect of bed depth on the breakthrough curves for  $\text{Nd}^{3+}$  and  $\text{Gd}^{3+}$  ion sorption onto Cyphos@silica material. In these investigations, the flow rate and initial feed concentration were fixed to 1 mL/min and 100 mg/L, respectively, for each metal ions solution. The column bed depth of 2.0 and 3.0 cm could be employed by packing the column with 0.79 and 1 gm of Cyphos@silica material, respectively. The total quantity sorbed of metal ions ( $q_{\text{tot}}$ , mg) in the column, for a specified feed concentration ( $C_0$ , mg/L) and flow rate ( $Q$ , mL/min) with the total flow time ( $t_{\text{tot}}$ , min), can be obtained by estimating the area under the breakthrough curve that represents the integration of the sorbed ion concentration

( $C_{\text{ads}}$ , mg/L) plotted versus time as presented in the consequent equation [29]:

$$q_{\text{tot}} = \frac{Q}{1000} \int_{t=0}^{t=\text{tot}} C_{\text{ads}} dt = \frac{Q}{1000} \int_{t=0}^{t=\text{tot}} (C_0 - C) dt. \quad (1)$$

The total amount of metal ions served to the column ( $X$ , mg) is calculated from the next equation:

$$X = \frac{C_0 V_{\text{eff}}}{1000}, \quad (2)$$

where  $V_{\text{eff}}$  is the volume of the effluent, mL. Ultimate uptake (or bed capacity of the column, mg/g) is defined as: the total amount of metal sorbed,  $q_{\text{tot}}$  per weight of sorbent,  $w$ , for the whole operation time as demonstrated by Eq. (3), and the percent column performance, % can be assessed from Eq. (4):

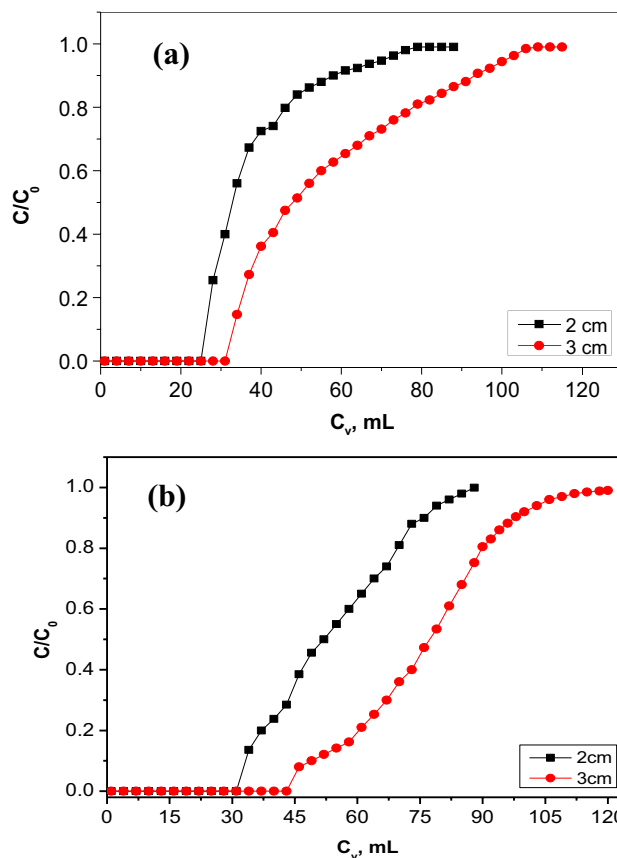
$$\text{Bed capacity} = \frac{q_{\text{tot}}}{w} \quad (3)$$

$$\text{Column performance (\%)} = \frac{q_{\text{tot}}}{X} \times 100. \quad (4)$$

Figure 1 illustrates that the shape of breakthrough curve differs with varying the bed depth. The bed capacity, breakthrough time, and the removal percent of  $\text{Nd}^{3+}$  and  $\text{Gd}^{3+}$  ions (column performance) increased with increasing the bed depth, as shown in Table 1. The increases in the sorbent doses in longer bed heights lead to increase in the bed capacity in longer bed heights, where higher surface area provided and consequently more sorption sites offered to the metal ions. The bed capacity for  $\text{Gd}^{3+}$  is greater than  $\text{Nd}^{3+}$ ; this may be due to the difference the ionic radius. Consequently, gadolinium ions (the smaller) can be easily sorbed than neodymium ions.

### Effect of Flow Rate

The influence of variable flow rate on sorption of  $\text{Nd}^{3+}$  and  $\text{Gd}^{3+}$  ions by Cyphos@silica material was investigated at different flow rates, 1.0 and 2.0 mL/min, whereas keeping the initial metal ion concentration at 100 mg/L and the bed depth of 3 cm. The plots of the breakthrough curves of  $\text{Nd}^{3+}$  and  $\text{Gd}^{3+}$  ions at the two flow rates are displayed in Fig. 2. The total sorbed ion quantities and column performance with respect to the two examined flow rates were estimated from the breakthrough curves and are listed in Table 2. From the data obtained, it was found that breakthrough curves become sharper at higher flow rates. With rising flow rate, the breakthrough time and the entire  $\text{Nd}^{3+}$  and  $\text{Gd}^{3+}$  ions sorbed decreased. This is certainly due to the reduced contact time that causes a weak distribution of the solution throughout the



**Fig. 1** Effect of bed depth on the breakthrough curve for sorption of **a**  $\text{Nd}^{3+}$  and **b**  $\text{Gd}^{3+}$  ions at flow rate 1.0 mL/min and initial concentration 100 mg/L

column, resulting in a lower diffusion of the solution onto the Cyphos@silica material particles.

Initially, the sorption was fast at a lower flow rate likely associated with the availability of reaction sites capable of capturing metal ions around or within the material particles. Due to the incremental occupation of these sites, the opportunity for sorption uptake becomes fewer in the next stage of the process.

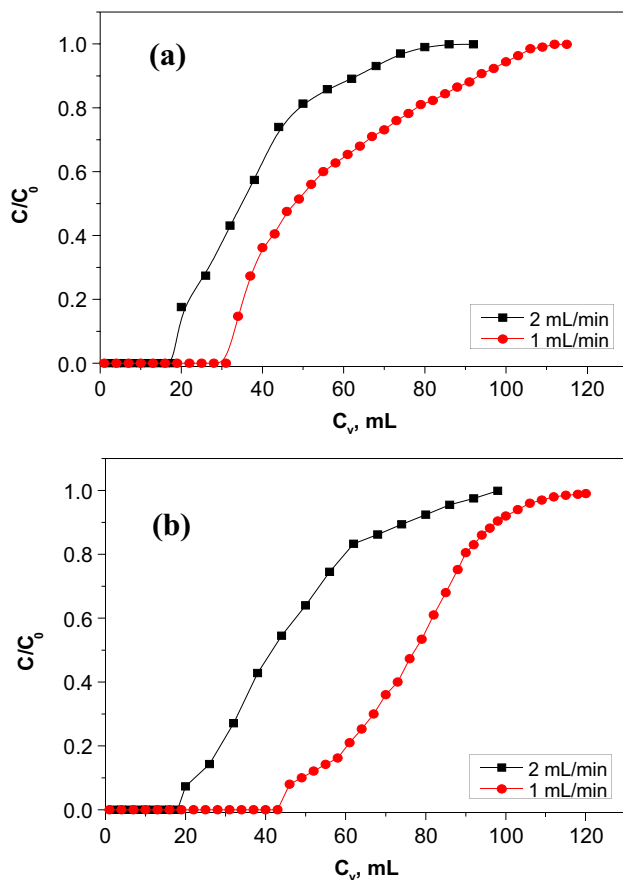
When the flow rate is increased, the breakthrough curve becomes steeper with which the breakpoint time and concentration of adsorbed ions decreases. This may explain the reason why the column performance is better at the slowest flow rate [30].

### Influence of Initial Feed Concentration

Two initial  $\text{Nd}^{3+}$  and  $\text{Gd}^{3+}$  ion concentrations were used for studying the sorption performance of Cyphos@silica column. The effect of varying the initial metal ion concentrations of 50 and 100 mg/L at a flow rate of 1.0 mL/min and bed depth of 3.0 cm is illustrated in Fig. 3. The total sorbed quantities and the removal percent (column performance)

**Table 1** Effect of bed depth on breakthrough capacity of Cyphos@silica for sorption of Nd<sup>3+</sup> and Gd<sup>3+</sup>

Metal ion	C <sub>0</sub> (mg/L)	Q (mL/min)	Z (cm)	X (mg)	q <sub>tot</sub> (mg)	Column performance (%)	Bed capacity (mg/g)
Gd <sup>3+</sup>	100	1	3	12	7.6	63.3	7.6
	100	1	2	10.3	5.38	50.2	6.8
Nd <sup>3+</sup>	100	1	3	11.2	5.4	48.2	5.4
	100	1	2	8.77	3.76	42.9	4.8

**Fig. 2** Effect of flow rate on the breakthrough curve for sorption of **a** Nd<sup>3+</sup> and **b** Gd<sup>3+</sup> ions at bed depth 3.0 cm and concentration 100 mg/L**Table 2** Effect of flow rate on breakthrough capacity for sorption of Nd<sup>3+</sup> and Gd<sup>3+</sup> onto Cyphos@silica

Metal ion	C <sub>0</sub> (mg/L)	Q (mL/min)	Z (cm)	X (mg)	q <sub>tot</sub> (mg)	Column performance (%)	Bed capacity (mg/g)
Gd <sup>3+</sup>	100	1	3	12	7.6	63.3	7.6
	100	2	3	9.8	3.7	37.7	3.7
Nd <sup>3+</sup>	100	1	3	11.2	5.4	48.2	5.4
	100	2	3	9.21	3.76	40.8	3.5

regarding the initial metal ions concentration were calculated and are represented in Table 3. As it is obvious from the figures, the increase in the initial Gd<sup>3+</sup> and Nd<sup>3+</sup> concentrations leads to reduction in the amount of solutions treated before breakthrough. This is because column bed saturated by the high concentration of metal ions. Concentration gradient between the concentration of metal ions in the bulk solution and in/inside the sorbent particles considered to be the essential forces that promote the sorption process. This may clarify the reason for acquiring greater sorption capacity of Nd<sup>3+</sup> and Gd<sup>3+</sup> at greater concentration of their solution fed to the column [31].

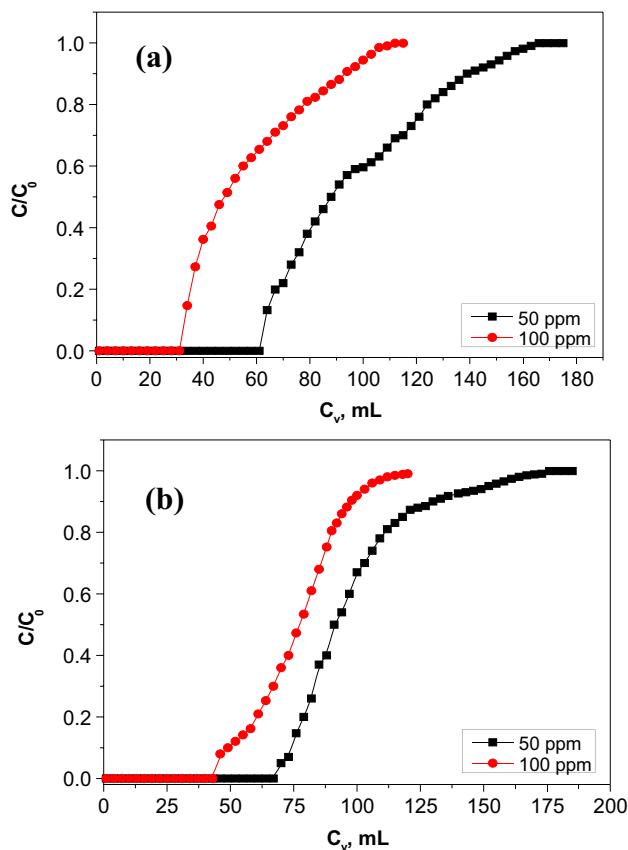
## Modeling of Breakthrough Curves

### Adams–Bohart Model

Adams–Bohart model [32] relies on the mechanism of reactions that occur on the surface. This model assumes first-order rate of reaction with respect to both solution concentration and free sites on the surface of sorbent. The adsorption rate is proportional to the adsorbent's available vacant sites. The equations describe the relation between normalized concentration ( $C_t/C_0$ ) and time could be described by this model. The application of the model is constrained on the first portion of the breakthrough curve. The kinetic and ultimate capacity parameters denoted by the symbols  $k_{AB}$  and  $N_0$  can be assessed using the following expression:

$$\ln \frac{C_t}{C_0} = k_{AB} C_0 t - k_{AB} N_0 \frac{Z}{F}, \quad (5)$$

where the concentration of the solution fed to and exiting the column is  $C_0$  and  $C_t$  (mg/L).  $k_{AB}$  (L mg<sup>-1</sup> min<sup>-1</sup>) is the



**Fig. 3** Effect of initial feed concentration on the breakthrough curve for sorption of **a** Nd<sup>3+</sup> and **b** Gd<sup>3+</sup> ions at bed depth 3.0 cm and flow rate 1.0 mL/min

kinetic constant,  $F$ , cm/min is the linear velocity,  $Z$ , cm is the column bed height, and  $N_0$ , mg/L is the maximum concentration. The validity of this model is restricted to the outlined conditions [33]. The values of  $N_0$  and  $k_{AB}$  can be gotten from the intercept and slope the linear plot of  $\ln(C_t/C_0)$  against time  $t$  as represented by Figs. 4, 5, and 6. The calculated values of these and the fitting correlation coefficients exist in Table 4.

As the data in Table 4 show, the values of  $k_{AB}$  increases with increasing the flow rate, but it is lessened with increasing bed height and the inlet concentration. The values of

$N_0$  increase with increasing the inlet concentration and bed height but decreasing with speeding the flow rate.

**Thomas Model**

The Thomas model is a common model that is broadly used for theoretical description of column performance. According to the assumption, axial and radial dispersion are neglected. It also assumes that the physical properties of both the sorbent and the solution do not change during the experiment [34]. The linearized formula of Thomas model can be expressed as follows:

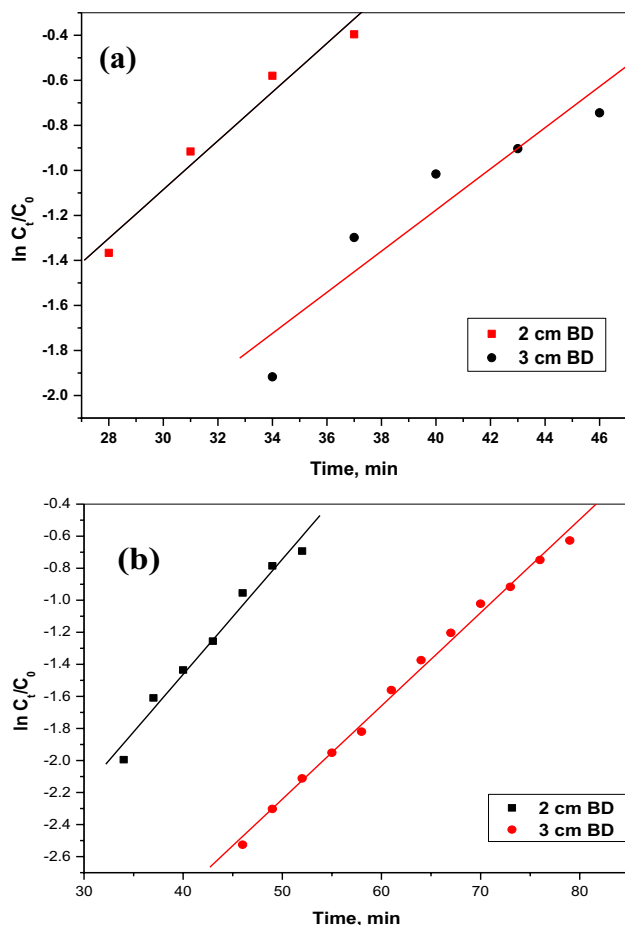
$$\ln\left(\frac{C_0}{C_t} - 1\right) = \frac{k_{Th}q_0M}{F} - \frac{k_{Th}C_0V}{F}, \tag{6}$$

where  $k_{Th}$ , mL/min.mg is the Thomas rate constant;  $q_0$ , mg/g is the metal ions uptake per g of the adsorbent at equilibrium;  $C_0$  (mg/L) is the influent metal ion concentration;  $C_t$  (mg/L) is the outlet concentration at certain time,  $t$ ;  $M$  (g) is the mass of sorbening material;  $F$ , (mL min<sup>-1</sup>) is the flow rate; and  $V$  (ml) is the throughput volume. The value of  $C_t/C_0$  is the proportion of outlet and influent ion concentrations. A linear plot of  $\ln(C_0/C_t) - 1$  versus effluent volume ( $V_{eff}$ ) was drawn to determine the values of  $k_{Th}$  and  $q_0$  from the slope and intercept of the plot as displayed by Figs. 7, 8, and 9. The values of concentration variance obtained from column experiments were fitted to the Thomas model. The constants,  $k_{Th}$  and  $q_0$ , resulting from linear fitting are presented in Table 5.

From Table 5, it is realized that values of  $R^2$  range from 0.93 to 0.98. Moreover, as the influent concentration increased, the value of  $q_0$  and  $k_{Th}$  increased. This increase is due to concentration gradient, while decreasing the values of  $q_0$  was observed when reducing the inlet solution flow rate. As the bed heights increased, the values of  $q_0$  increased and  $k_{Th}$  decreased. It is also interestingly observed from the data summarized in Table 5, the  $q_0$  values calculated from the Thomas model is very close to the experimental termed as  $q_{c(expt)}$ . These findings proved the appropriateness of Thomas model for acquiring the sorption processes where the external and internal diffusions will not be the limiting step [35].

**Table 3** Effect of initial feed concentration on breakthrough capacity for sorption of Nd<sup>3+</sup> and Gd<sup>3+</sup> onto cyphos@silica

Metal ion	C <sub>0</sub> (mg/L)	Q (mL/min)	Z (cm)	X (mg)	q <sub>total</sub> (mg)	Column performance (%)	Bed capacity (mg/g)
Gd <sup>3+</sup>	50	1	3	9.2	4.86	52.7	4.86
	100	1	3	12	7.6	63.3	7.6
Nd <sup>3+</sup>	50	1	3	8.3	4.5	54	4.5
	100	1	3	11.2	5.4	48.2	5.4

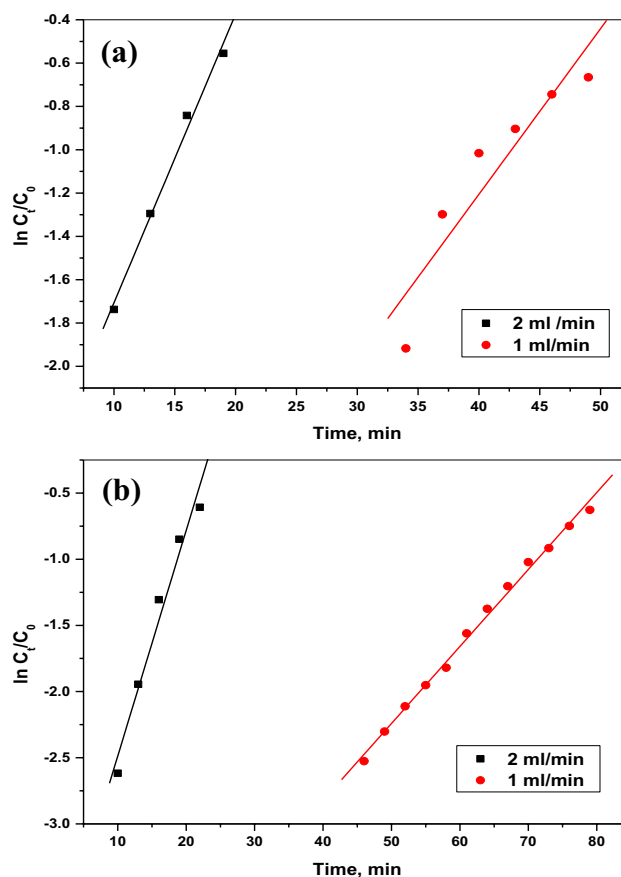


**Fig. 4** Adams–Bohart model plots for sorption of **a**  $\text{Nd}^{3+}$  and **b**  $\text{Gd}^{3+}$  onto cyphos@silica at various bed depths

### Comparison of Batch and Fixed Bed Kinetics of Sorption Process

Batch and column experiments are commonly performed for determining the characteristics of the materials used as sorbents and for evaluation of the whole sorption process. In practical applications, the sorption process may be performed as batch or dynamic continuous operation. The two operations have many advantages in common such as simple to operate and ability of using a wide variety of media, but column operation can be operated at elevated temperatures and offer the advantage of reaching high decontamination factor. Column process may be considered as series of batch operations and such system used frequently in treating radioactive liquid wastes [36, 37].

Kinetics data of sorption of  $\text{Gd}^{3+}$  and  $\text{Nd}^{3+}$  in batch mode investigated in our previous work [2] have been tested to Thomas and Adams–Bohart models (Figs. 10, 11). Modified equation of Thomas model for batch adsorption [38] is expressed as follows:



**Fig. 5** Adams–Bohart model plots for sorption of **a**  $\text{Nd}^{3+}$  and **b**  $\text{Gd}^{3+}$  onto cyphos@silica at different flow rates

$$\frac{C}{C_0} = \exp\left(k_{\text{Th}}\left(\frac{1-\varepsilon}{\varepsilon} \rho q_0 - C_0\right)t\right), \quad (7)$$

where  $\rho$  is the density of the sorbent material and  $\varepsilon$  is the liquid volume fraction. The tested sorption data of  $\text{Gd}^{3+}$  and  $\text{Nd}^{3+}$  onto the impregnated silica could not fit this form of Thomas model.

Adams–Bohart model rate model relies on surface reaction mechanism. This model assumes first order of reaction with respect to both solution concentration and free sites on the surface of sorbent [39]. Loebenstein et al. [40, 41] develop a solution of both rate and mass conservation equation:

$$C = C_0 - C_0 A \left[ \frac{1 - \exp\left[(A-1)C_0 k_{\text{AB}} t\right]}{1 - A \exp\left[(A-1)C_0 k_{\text{AB}} t\right]} \right], \quad (8)$$

where

$$A = \frac{M q_0}{V C_0}. \quad (9)$$



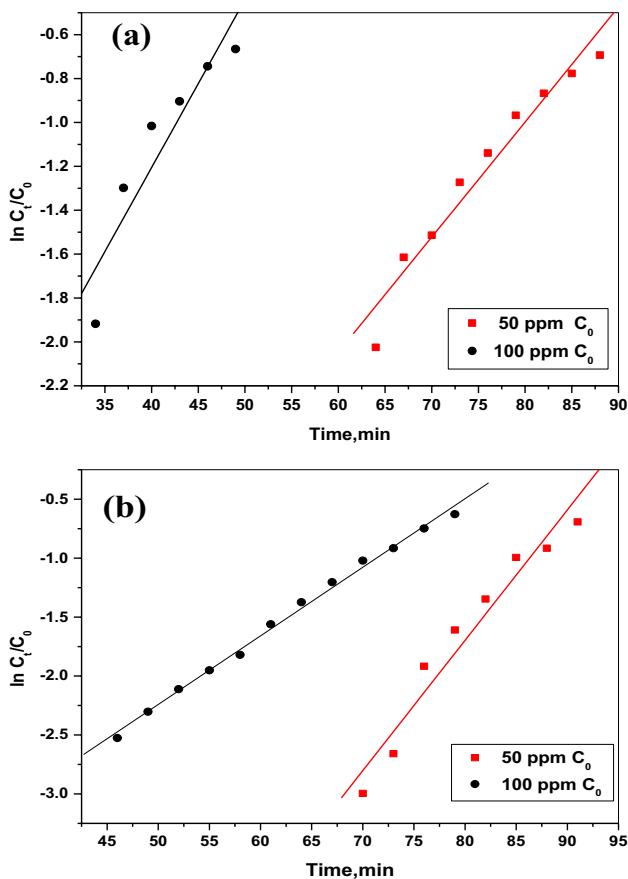


Fig. 6 Adams–Bohart model plots for sorption of **a** Nd<sup>3+</sup> and **b** Gd<sup>3+</sup> onto cyphos@silica at initial feed concentrations

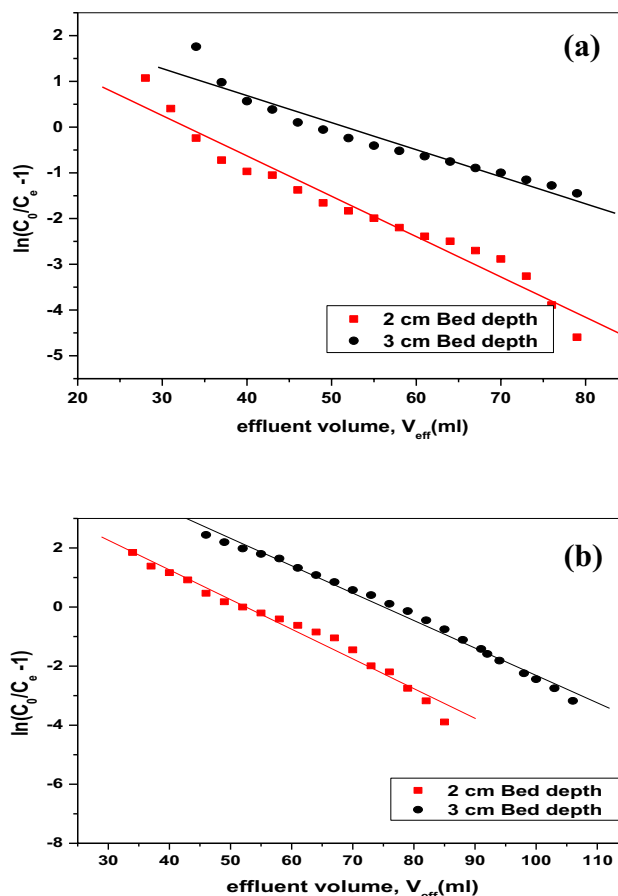


Fig. 7 Thomas model plots for sorption of **a** Nd<sup>3+</sup> and **b** Gd<sup>3+</sup> onto cyphos@silica at different bed depths

Table 4 Linear regression analysis of sorption data of Nd<sup>3+</sup> and Gd<sup>3+</sup> onto Cyphos@silica fitted to Adam’s–Bohart model

C <sub>0</sub> (mg/L)	Z (cm)	v (mL/min)	K <sub>AB</sub> (L mg <sup>-1</sup> min <sup>-1</sup> )	N <sub>0</sub> (mg/L)	R <sup>2</sup>
<b>Nd<sup>3+</sup></b>					
100	2	1	0.00128	2438	0.99
100	3	1	0.00051	2568	0.95
100	3	2	0.00133	1937	0.99
50	3	1	0.00076	2367	0.95
<b>Gd<sup>3+</sup></b>					
100	2	1	0.00072	3735	0.98
100	3	1	0.00058	4416	0.99
100	3	2	0.00171	2088	0.97
50	3	1	0.00058	4053	0.95

Equation in linear form could be expressed as follows:

$$\frac{1}{(A - 1)C_0} \ln \left( \frac{(A - 1)C_0 + C}{A C} \right) = k_{AB} t. \tag{10}$$

Plotting of the left-hand side of Eq. (10) vs *t* should be linear with slope of *k*<sub>AB</sub>, rate constants, and maximum capacities of sorption of the impregnated silica toward both metal ions (Table 6).

It can be noticed from the predicted kinetic data by Adams–Bohart model that sorption rate of batch mode sorption is higher than that of sorption by continuous mode using fixed bed column. This may be because the agitation applied during batch experiment led to break of the boundary layer around the sorbent particles.

### Separation of Gadolinium and Neodymium

Separation of Gd<sup>3+</sup> and Nd<sup>3+</sup> investigated using a column contains the prepared material, Cyphos@silica. The column packed with the material loaded by a mixture of both Gd<sup>3+</sup> and Nd<sup>3+</sup> ions solution (5.0 mL of 100 mg/L concentration of each). The experiment was performed at flow rate 1 mL/min and bed depth 3 cm. The separation process was first tested for elution of the two metal ions using distilled water and no release of any ions was observed for elution by

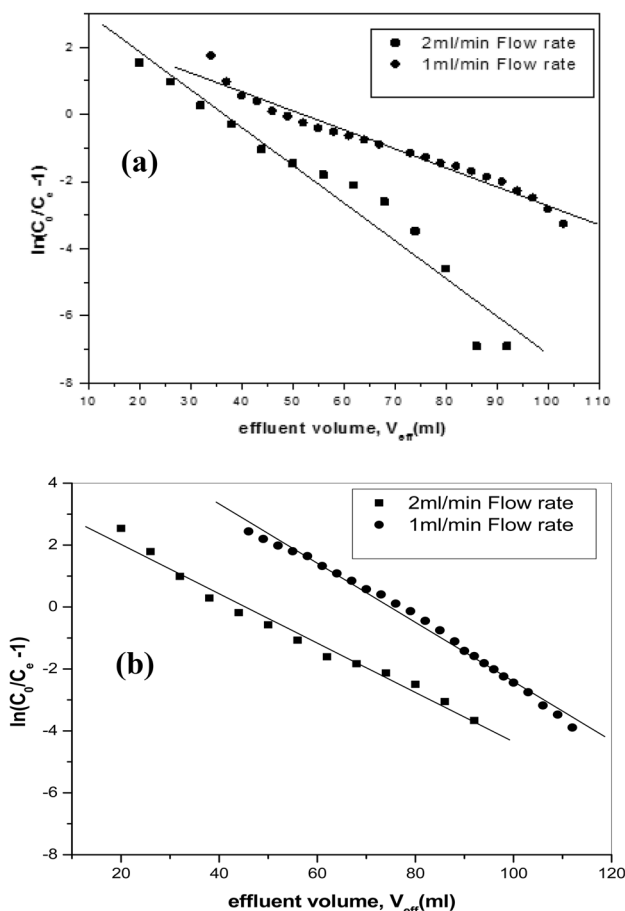


Fig. 8 Thomas model plots for sorption of a Nd<sup>3+</sup> and b Gd<sup>3+</sup> onto cyphos@silica at different flow rates

distilled water, and also NaOH solution cannot be used due to precipitation of lanthanides in basic media. 1.0 M nitric acid was found to be the best reagent for elution of Gd<sup>3+</sup> and Nd<sup>3+</sup>, as shown in Fig. 12.

Table 5 Thomas model parameters at different conditions for the sorption of Nd<sup>3+</sup> and Gd<sup>3+</sup> onto Cyphos@silica: linear regression

	C <sub>0</sub> (mg/L)	Z (cm)	v (mL/min)	K <sub>Th</sub> (L mg <sup>-1</sup> min <sup>-1</sup> ) × 10 <sup>3</sup>	q <sub>0</sub> (mg/g)	R <sup>2</sup>	q <sub>c</sub> (exp) (mg/g)
Nd <sup>3+</sup>							
Exp1	100	2	1	0.882	4.158	0.95	4.8
Exp2	100	3	1	0.566	5.191	0.93	5.6
Exp3	100	3	2	2.251	3.658	0.97	3.5
Exp4	50	3	1	0.497	4.66	0.97	4.86
Gd <sup>3+</sup>							
Exp1	100	2	1	1.005	6.648	0.98	6.8
Exp2	100	3	1	1.002	7.473	0.99	7.6
Exp3	100	3	2	1.594	4.537	0.98	3.7
Exp4	50	3	1	0.974	4.838	0.94	4.6

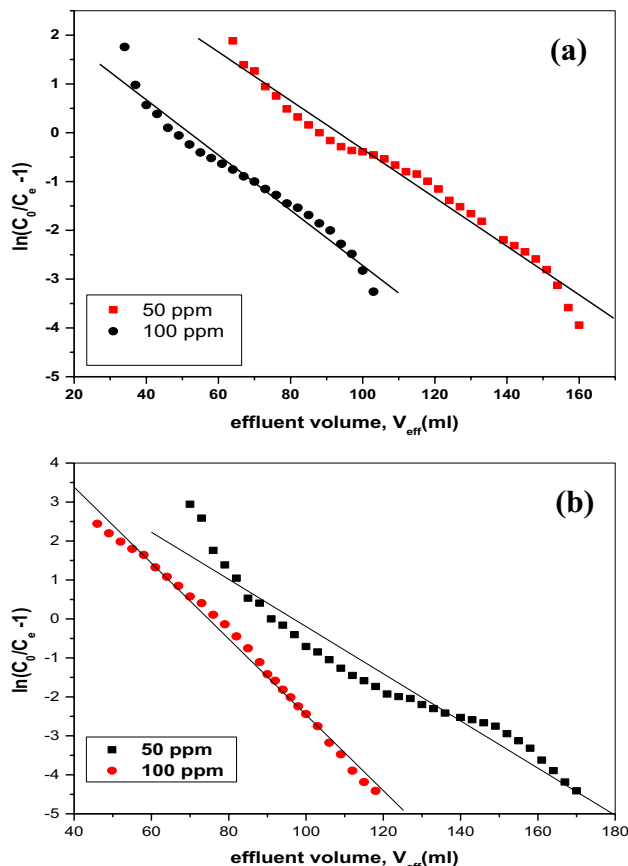


Fig. 9 Thomas model plots for sorption of a Nd<sup>3+</sup> and b Gd<sup>3+</sup> onto cyphos@silica at different initial feed concentrations

### Comparison of Sorption Capacity of Gd<sup>3+</sup> and Nd<sup>3+</sup> on Cyphos@silica with Other Sorbents

The sorption capacity of cyphos@silica toward Gd<sup>3+</sup> and Nd<sup>3+</sup> ions was compared to that of few sorbents in the literature, since there are very few investigations that calculated the sorption capacity of neodymium and/or gadolinium ions



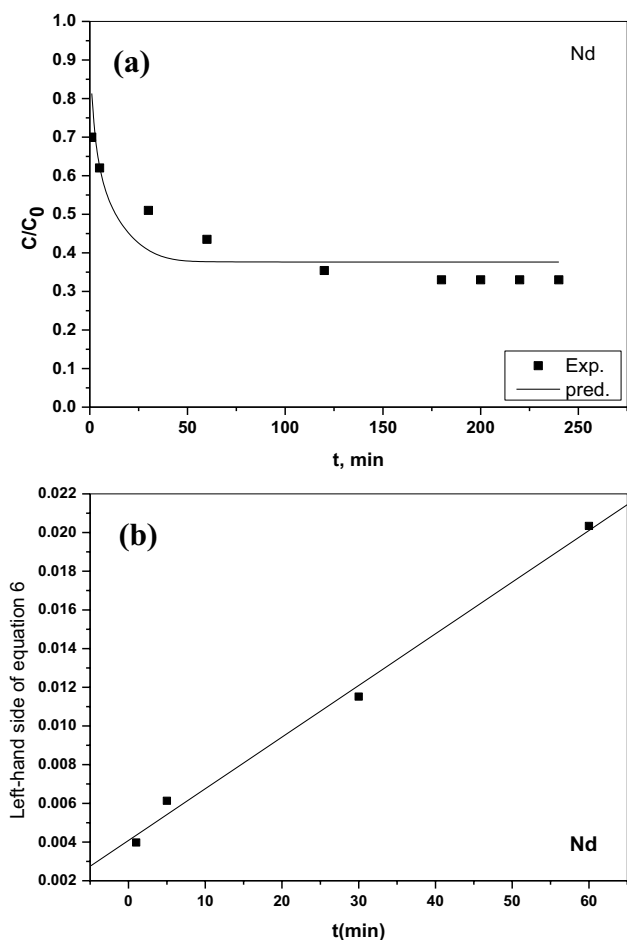


Fig. 10 Kinetic data of  $\text{Nd}^{3+}$  sorption onto cyphos@silica using Adams–Bohart equation: a Eq. 8 and b Eq. 10

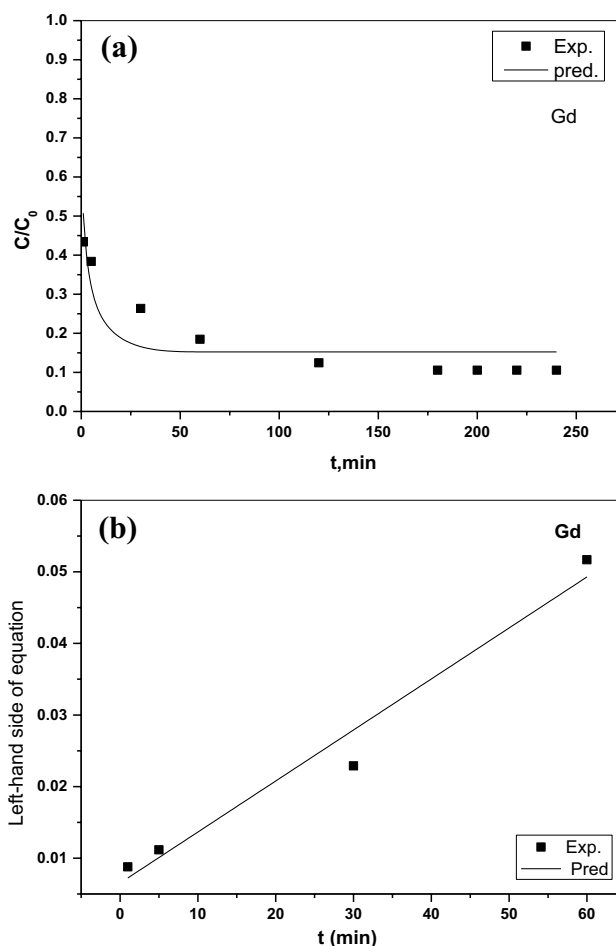


Fig. 11 Kinetic data of  $\text{Gd}^{3+}$  sorption onto cyphos@silica using Adams–Bohart equations: a Eq. 8 and b Eq. 10

Table 6 Parameters estimated by fitting the batch kinetic data to non-linear and linear forms of Adam–Bohart equations

Parameters	Metal ions	
	$\text{Nd}^{3+}$	$\text{Gd}^{3+}$
Nonlinear fitting		
$k_{AB}$ ( $\text{L mg}^{-1} \text{min}^{-1}$ )	0.0019	0.0063
$q_{0 \text{ pred.}}$ (mg/g)	12.47	16.95
$q_{0 \text{ exp}}$ (mg/g)	13.40	17.89
Linear fitting		
$k_{AB}$ ( $\text{L mg}^{-1} \text{min}^{-1}$ )	0.0003	0.0007

using fixed bed column. This gives an importance to this study. Table 6 displays that the cyphos@silica has higher sorption capacity than a sorbent, especially for gadolinium, and others have sorption capacity higher than that of cyphos@silica, but cyphos@silica is characterized by its efficiency for the separation of gadolinium and neodymium

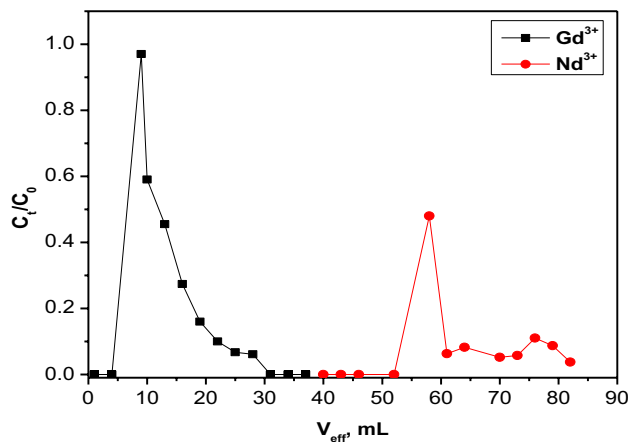


Fig. 12 Separation of  $\text{Nd}^{3+}$  and  $\text{Gd}^{3+}$  at 1.0 mL/min flow rate, 3.0 cm bed depth, and 1.0 M  $\text{HNO}_3$  medium

ions from each other. While there are many research articles using the batch technique for the removal of  $\text{Gd}^{3+}$  and

**Table 7** Comparison of sorption capacity of Nd<sup>3+</sup> and Gd<sup>3+</sup> onto different sorbents

Sorbents	Experimental conditions	Capacity, mg/g		References
		Nd <sup>3+</sup>	Gd <sup>3+</sup>	
cyphos@silica	pH=4.0	5.6	7.6	Present work
Sonicated Emulsion Polymer	pH=5.0	NR*	16.2	[42]
Phosphorus Functionalized Adsorbent	pH=6.0	47.5	NR*	[43]
Dowex-HCR-S/S	pH=4.0	NR*	66.0	[44]
Impregnated Amberlite XAD-4	pH=5.5	NR*	4.44	[45]

\*NR refers to not reported

Nd<sup>3+</sup> ions. In the previous work [2], the sorption capacity of cyphos@silica obtained from the batch technique was compared with that of other sorbents in the literature, the data revealed that cyphos@silica has much higher sorption capacity than many sorbents. Hence, cyphos@silica is considered as an encouraging sorbent for the removal and separation of gadolinium and neodymium ions (Table 7).

## Conclusion

In the present work, separation of Gd<sup>3+</sup> and Nd<sup>3+</sup> in was examined in fixed bed mode. Cyphos 104 impregnated silica was used as sorbent. Effect of influent flow rate, bed size, and initial ion concentration on breakthrough curves were considered. It was observed that the sorption capacity was higher at lower flow rate, higher bed depth, and initial ions concentration. The laboratorial data of the column were modeled using Thomas model and Adams–Bohart model. 1.0 M nitric acid was found to be efficient in separating both ions from binary mixture. The experimental data were in good agreement with theoretical results. The study revealed that Cyphos 104 impregnated silica packed in column can be used as an effective sorbent for the removal and separation of Gd<sup>3+</sup> and Nd<sup>3+</sup> from aqueous solution.

## Compliance with ethical standards

**Conflict of interest** The authors declare that there is no conflict of interest.

**Ethical approval** This article does not contain any studies with human participants or animals performed by any of the authors.

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